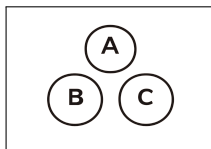


10 Discrete Distribution Posterior Probabilities

O

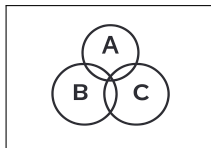


$$P(H) = 0.30$$

$$P(L) = 0.70$$

$$P(A|H) = 0.40$$

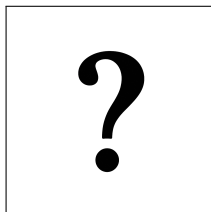
$$P(A|L) = 0.20$$



$$P(A) = P(A|H)P(H) + P(A|L)P(L)$$

$$P(A) = (0.4)(0.3) + (0.2)(0.7) = 0.12 + 0.14 = 0.26$$

$$P(H|A) = \frac{P(A|H)P(H)}{P(A)} = \frac{(0.4)(0.3)}{0.26} = \frac{0.12}{0.26} = \frac{6}{13} \approx 0.4615$$



$$P(A) = 0.60$$

$$P(S) = 0.30$$

$$P(N) = 0.10$$

$$P(X|A) = 0.80$$

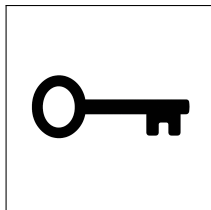
$$P(X|S) = 0.60$$

$$P(X|N) = 0.40$$

$$P(A|X) = ?$$

10 Discrete Distribution Posterior Probabilities

O



$$P(A) = 0.60$$

$$P(S) = 0.30$$

$$P(N) = 0.10$$

$$P(X|A) = 0.80$$

$$P(X|S) = 0.60$$

$$P(X|N) = 0.40$$

$$P(A|X) = ?$$

$$\begin{aligned} P(X) &= P(X|A)P(A) + P(X|S)P(S) + P(X|N)P(N) \\ &= (0.80)(0.60) + (0.60)(0.30) + (0.40)(0.10) \\ &= 0.70 \end{aligned}$$

$$P(A|X) = \frac{P(X|A)P(A)}{P(X)} = \frac{(0.80)(0.60)}{0.70} = 0.69$$